

- 3 (b) A particle is projected down an inclined plane with initial velocity  $u$  m/s. The line of projection makes an angle of  $2\theta^\circ$  with the inclined plane and the plane is inclined at  $\theta^\circ$  to the horizontal. The plane of projection is vertical and contains the line of greatest slope.

The range of the particle on the inclined plane is  $\frac{ku^2}{g} \sin \theta$ .

Find the value of  $k$ .

$$r_j = 0$$

$$0 = u \sin 2\theta \cdot t - \frac{1}{2} g \cos \theta \cdot t^2$$

$$\Rightarrow t = \frac{2u \sin 2\theta}{g \cos \theta} \text{ or } \frac{4u \sin \theta}{g}$$

$$\text{Range} = u \cos 2\theta \left\{ \frac{4u \sin \theta}{g} \right\} + \frac{1}{2} g \sin \theta \left\{ \frac{4u \sin \theta}{g} \right\}^2$$

$$= \frac{4u^2}{g} \{ \cos 2\theta \sin \theta + 2 \sin \theta \sin^2 \theta \}$$

$$= \frac{4u^2}{g} \{ (\cos^2 \theta - \sin^2 \theta) \sin \theta + 2 \sin^3 \theta \}$$

$$= \frac{4u^2}{g} \{ \cos^2 \theta \sin \theta + \sin^3 \theta \}$$

$$= \frac{4u^2}{g} \{ \sin \theta (\cos^2 \theta + \sin^2 \theta) \}$$

$$= \frac{4u^2 \sin \theta}{g}$$

$$\Rightarrow k = 4$$

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