

- (b) 2000 A particle is projected at an angle $\alpha = \tan^{-1} 3$ to the horizontal up a plane inclined at an angle θ to the horizontal. (The plane of projection is vertical and contains the line of greatest slope). The particle strikes the plane at right angles.

Find two possible values for θ .

$$r_j = u \sin(\alpha - \theta).t - \frac{1}{2} g \cos \theta . t^2$$

$$v_i = u \cos(\alpha - \theta) - g \sin \theta . t$$

$$r_j = 0 \Rightarrow t = \frac{2u \sin(\alpha - \theta)}{g \cos \theta}$$

$$v_i = 0 \Rightarrow t = \frac{u \cos(\alpha - \theta)}{g \sin \theta}$$

$$\frac{2u \sin(\alpha - \theta)}{g \cos \theta} = \frac{u \cos(\alpha - \theta)}{g \sin \theta}$$

$$2 \tan(\alpha - \theta). \tan \theta = 1$$

$$2 \left\{ \frac{\tan \alpha - \tan \theta}{1 + \tan \alpha . \tan \theta} \right\} \tan \theta = 1 \Rightarrow 2 \left\{ \frac{3 - \tan \theta}{1 + 3 \tan \theta} \right\} \tan \theta = 1$$

$$2 \tan^2 \theta - 3 \tan \theta + 1 = 0$$

$$\Rightarrow \tan \theta = \frac{1}{2} \text{ or } \tan \theta = 1$$

$$\Rightarrow \theta = 26.6^\circ \text{ or } 45^\circ$$

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