

3. (a)

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A particle is projected with a velocity of  $u$  m/s at an angle  $\beta$  to the horizontal ground.

Show that the particle hits the ground at a distance  $\frac{u^2}{g} \sin 2\beta$  from the point of projection.

Find the angle of projection which gives maximum range.

$$\vec{r} = (u \cos \beta \cdot t) \vec{i} + (u \sin \beta \cdot t - \frac{1}{2} g t^2) \vec{j}$$

$$r_j = 0 \Rightarrow t = \frac{2 u \sin \beta}{g}$$

$$\text{Range} = u \cos \beta \left( \frac{2 u \sin \beta}{g} \right) = \frac{u^2 \sin 2\beta}{g}$$

$$\text{For max range } \sin 2\beta = 1 \text{ or } \frac{dR}{d\beta} = \frac{u^2 \cos 2\beta (2)}{g} = 0$$

$$\Rightarrow \beta = 45^\circ$$

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