

KINETIC ENERGY:

You must be very careful if asked about the kinetic energy lost or gained in a ~~problem~~ collision as to what exactly you are being asked!

→ The kinetic energy of a body ^{mass 5kg} moving with velocity $3\hat{i} - 14\hat{j}$ is

$$= \frac{1}{2} m v^2 = \frac{1}{2} 5 (\sqrt{3^2 + (-14)^2})^2$$

$$= \frac{5}{2} (3^2 + 14^2)$$

$$= \frac{5}{2} (203) = 507.5 \text{ Joules}$$

→ The kinetic energy lost by the left body in the "Impulse Eq" if we take $m_1 = 10$.

$$\frac{1}{2} m_1 v_1^2 - \frac{1}{2} m_1 u_1^2 = \frac{1}{2} 10 (3^2 + 7^2) - \frac{1}{2} 10 ((-6)^2 + 7^2)$$

$$= 5(9 + 49) - 5(36 + 49)$$

$$= 45 + 245 - 180 - 245$$

$$= -135 \text{ Joules}$$

What do you notice about the KE change in the 'j' components?

→ The total kinetic energy lost by the system in the "Impulse Eq" (Take $m_2 = 12$)

is Total KE After - Total KE Before

$$= \left[\frac{1}{2} 10 (3^2 + 7^2) + \frac{1}{2} 12 ((-2)^2 + 3^2) \right] - \left[\frac{1}{2} 10 ((-6)^2 + 7^2) + \frac{1}{2} 12 (1^2 + 3^2) \right]$$

$$= [5(9 + 49) + 6(4 + 9)] - [5(36 + 49) + 6(1 + 9)]$$

$$= 5(9) + 5(49) + 6(4) + 6(9) - 5(36) - 5(49) - 6(1) - 6(9)$$

$$= 5(9) - 5(36) + 6(4) - 6(1)$$

$$= 45 - 180 + 24 - 6$$

$$= -135 + 18$$

$$= -117 \text{ Joules}$$

[Again what do you notice about the 'j' part contribution to the energies change?]

→ The fractional change of kinetic energy of one of the spheres

~~ΔKE~~ = FRACTIONAL CHANGE = $\frac{\Delta KE}{\text{old KE}} = \frac{\text{Change in KE}}{\text{original KE}}$

NB: As we have seen so far we can 'forget' the 'j' components contribution to the KE when calculating the top line ΔKE as they cancel each other out BUT in the subtraction no subtraction to cancel any (they out)