A smooth sphere, of mass m, moving with velocity $6\vec{i} + 2\vec{j}$ collides with a smooth sphere, of mass km, moving with velocity $2\vec{i} + 4\vec{j}$ on a smooth horizontal table.

2 1 4 1 2

After the collision the spheres move in parallel directions.

The coefficient of restitution between the spheres is *e*.

- (i) Find e in terms of k.
- (ii) Prove that $k \ge \frac{1}{3}$.

PCM

NEL

$$m(6) + km(2) = mv_1 + kmv_2$$

$$v_1 - v_2 = -e(6-2)$$

$$v_1 = \frac{6 + 2k - 4ek}{k+1}$$

$$v_2 = \frac{6 + 4e + 2k}{k+1}$$

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parallel directions ⇒ slopes are equal

$$\frac{2}{v_1} = \frac{4}{v_2}$$

$$v_2 = 2v_1$$

$$\frac{6+4e+2k}{k+1} = \frac{2(6+2k-4ek)}{k+1}$$

$$3+2e+k = 6+2k-4ek$$

$$e = \frac{3+k}{2+4k}$$

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(ii)

$$e \le 1$$

$$\frac{3+k}{2+4k} \le 1$$

$$3+k \le 2+4k$$

$$k \ge \frac{1}{3}$$

5

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