

2007

3.

(a)

A particle is projected with a speed of $7\sqrt{5}$ m/s at an angle α to the horizontal.

Find the two values of α that will give a range of 12.5 m.

$$r_j = 0$$

$$7\sqrt{5} \sin \alpha \cdot t - \frac{1}{2}gt^2 = 0$$

$$\Rightarrow t = \frac{14\sqrt{5} \sin \alpha}{g}$$

$$\text{Range} = 7\sqrt{5} \cos \alpha \cdot t$$

$$= 7\sqrt{5} \cos \alpha \cdot \left(\frac{14\sqrt{5} \sin \alpha}{g} \right)$$

$$= 50 \sin \alpha \cos \alpha$$

$$= 25 \sin 2\alpha$$

$$\text{Range} = 12.5$$

$$25 \sin 2\alpha = 12.5$$

$$\sin 2\alpha = \frac{1}{2}$$

$$\Rightarrow 2\alpha = 30^\circ \text{ or } 150^\circ$$

$$\Rightarrow \alpha = 15^\circ \text{ or } 75^\circ$$

5

5

5

5

5

25