

(98)

6 (a) Define Simple Harmonic Motion.

The distance, x , of a particle from a fixed point, o , is given by
 $x = 7\sin \omega t + 24 \cos \omega t$, ω being a constant.

- (i) Show that the particle is describing simple harmonic motion about o .
- (ii) Calculate the amplitude of the motion.

The motion of a particle is simple harmonic motion if its acceleration towards a particular point is proportional to its displacement from that point.

(i) $x = 7 \sin \omega t + 24 \cos \omega t$

$$\frac{dx}{dt} = 7\omega \cos \omega t - 24\omega \sin \omega t$$

$$\frac{d^2x}{dt^2} = -7\omega^2 \sin \omega t - 24\omega^2 \cos \omega t$$

$$= -\omega^2 x$$

\therefore S.H.M. about $x = 0$

(ii) amplitude $= \sqrt{7^2 + 24^2}$

$$= 25$$

10

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