

5 PCM

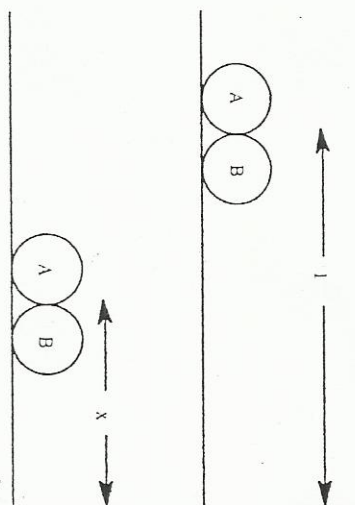
$$mu + 0 = mv_1 + mv_2 \Rightarrow v_1 + v_2 = u$$

NEL

$$v_1 - v_2 = -e(u - 0) \Rightarrow v_1 - v_2 = -eu$$

$$v_1 = \frac{u}{2}(1 - e)$$

$$v_2 = \frac{u}{2}(1 + e)$$



B strikes the wall with velocity $\frac{u}{2}(1 + e)$ and rebounds with velocity $\frac{eu}{2}(1 + e)$

$$\frac{1 - x}{\frac{u}{2}(1 - e)} = \frac{1}{\frac{u}{2}(1 + e)} + \frac{x}{\frac{eu}{2}(1 + e)}$$

$$x = \frac{2e^2}{1 + e^2}$$

OR Time for B to reach the wall = $\frac{\text{distance}}{\text{speed}} = \frac{1}{\frac{u}{2}(1 + e)} = \frac{2}{u(1 + e)}$

$$\text{In this time A travels } \frac{u(1 - e)}{2} \cdot \frac{2}{u(1 + e)} = \frac{1 - e}{1 + e}$$

$$\text{and is now } 1 - \frac{1 - e}{1 + e} = \frac{2e}{1 + e} \quad \text{from the wall}$$

$$\text{B's rebound velocity is } \frac{eu}{2}(1 + e)$$

$$\frac{x}{\frac{eu}{2}(1 + e)} = \frac{\frac{2e}{1 + e} - x}{\frac{u}{2}(1 - e)}$$

$$x = \frac{2e^2}{1 + e^2}$$

1620 RE

6 (i)

$$\text{amplitude} = (1.5 - 0.9) \div 2 = 0.3 \text{ metres}$$

$$\text{Period} = \frac{2\pi}{\omega} = \frac{\pi}{6} \Rightarrow \omega = 12 \text{ rad/s}$$

$$\text{max speed} = \omega a = 12 \times 0.3 = 3.6 \text{ m/s}$$

(ii) Maximum force that the glue has to exert is at the highest point, when

$$\begin{aligned} \text{maximum acceleration} &= \omega^2 a \\ &= 144 \times 0.3 \\ &= 43.2 \text{ (downwards)} \end{aligned}$$

Let F be the force that the glue exerts on Q

$$\text{Force} = \text{mass} \times \text{acceleration}$$

$$mg + F = m\ddot{a}$$

$$0.2(9.8) + F = 0.2(43.2)$$

$$F = 6.68 \text{ N}$$

(iii) In the absence of glue, Q will leave the pan when $R = 0$

$$mg - R = m\ddot{a}$$

$$mg - 0 = m\omega^2 x$$

$$9.8 = 144x$$

$$x = 0.068 \text{ m}$$

$$\Rightarrow \text{length of spring} = 1.2 - 0.068 = 1.132 \text{ m}$$